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**Matti Pajari**

# **Prestressed hollow core slabs supported on beams**

**Finnish shear tests on floors in 1990–2006**



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#### **Title Prestressed hollow core slabs supported on beams Finnish shear tests on floors in 1990–2006**

**Abstract** 

Arrangements and results of 20 full-scale load tests on floors, each made of eight to twelve prestressed hollow core slabs and three beams, are presented. The tests have been carried out by VTT Technical Research Centre of Finland and Tampere University of Technology.

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### **Preface**

The reduction of the shear resistance of hollow core slabs due to deflection of the supporting beams has been studied since 1990. Despite numerous tests, theoretical and numerical analyses and international cooperation, no common European understanding about the reasons of and solutions for this phenomenon has been achieved. A German research project "*Querkrafttragfähigkeit von Spannbeton-Fertigdecken bei biegeweicher Lagerung*", recently completed at Institut für Massivbau, Rheinisch-Westfälische Technische Hochschule, Aachen, aimed to be a step to that direction. The present report has been elaborated as a part of this project.

All reported tests have been performed in confidential projects and commissions. The owners of the results mentioned in the report have permitted the publication of all relevant data and paid the costs of the information service, which is gratefully acknowledged.

The work has financially been supported by the research team in Aachen, i.e. Prof. Hegger, Dr. Roggendorf and their coworkers. Without their contribution it would not have been possible to realise the work. Special thanks are due to them for their patience in waiting for the completion of the report and for the kind and encouraging atmosphere before, during and after the project.

## **Contents**



## **Meaning of abbreviations**



### **1. Introduction**

The effect of flexible supports, i.e. reduction of the shear resistance of the hollow core slabs due to deflection of the supporting beams, has been experimentally studied since 1990. The results and analysis of ten tests carried out by VTT, Finland, have been published previously. Due to these tests and parallel tests performed elsewhere it has become clear that the reduction of the shear resistance has to be taken into account in design.

European standard EN 1168. *Precast concrete products. Hollow core slabs* has been amended by a sentence stating that the effect of flexible supports on the shear resistance shall be taken into account. How this can be done, is not specified. Therefore, national design rules, if any, are applied to meet this requirement. It is obvious that a European design method has to be developed, but this is not only a question of standardisation; research is also needed.

In 2005, a research project dealing with the effects of flexible supports was started at RWTH, Aachen. New floor tests were performed, but the results of the former Finnish and German tests were also considered. As a part of the project, the test arrangements and results of twenty Finnish floor tests in 1990–2006 have been elaborated and published in this report. The aim has been to provide experimental data which can be referred to when writing scientific papers or when developing and standardizing European design rules. No analysis of the results is presented. The aim has also been to make the data so complete that there is no need to read the original test reports, five of which have been written in Finnish. Some tabulated characteristics of the tests are given on the first page. The rest of the report is divided in 20 Chapters, each including the results on one floor test and the related reference tests.

The German test results are available at

#### [http://www.imb.rwth-aachen.de/Weitere-Informationen/](http://sisis.bth.rwth-aachen.de:8080/InfoGuideClient/start.do)

(Titel "Zum Tragverhalten von Spannbeton-Fertigdecken bei biegeweicher Lagerung")

## **2. Summary**

Basic data about the tests are given in Table 1.

Table 1. Thickness of slabs ( $h_{slab}$ ), length of core filling ( $L_{fill}$ ), span of beams (L), length of slabs  $(L_{slab})$ , shear resistance / one slab in floor test ( $V_{obs}$ ), mean of shear resistances observed in reference tests ( $V_{ref}$ ) and last measured deflection of the middle beam before failure ( $\delta$ ).



<sup>1)</sup> Last measured deflection before failure

<sup>2)</sup> Deflection at failure  $> 5.4$  mm and  $< 7.2$  mm

**3. Shear tests on floors** 











*Fig. 11. Loading arrangement with three layers of spreader beams.* 













*Fig. 17. Slab 1 after failure.* 



*Fig. 18. Top surface of slabs 1 (on the left), 2 and 3 after failure.* 































#### VTT.S.WQ.265.1990
















*Fig. 13. Failure of slabs 8 and 7.* 






























































VTT.PC.InvT.265.1990



74



















*Fig. 14. Failure of slab 4.*



*Fig. 15. Cracks parallel to beam. South end of middle beam.* 



*Fig. 16. Failure of slabs 1 (on the right) and 5 (on the left).*



*Fig. 17. Cracks after failure in slab 8 and in the joint concrete.* 



*Fig. 18. Failure of slab 1.*



*Fig. 19. Failure of slab 5.* 



*Fig. 20. Cracks parallel to beam in joint concrete. North end of middle beam.*





## VTT.PC.InvT.265.1990





















## VTT.PC.InvT.265.1990
























## VTT.PC.InvT.400.1992













*Fig. 30. Deflection on line III.* 



*Fig. 31. Deflection on line IV, middle beam.* 









*Fig. 34. Deflection on line VIII along Eastern end beam.*









## **10.5 Strain**

A gradual growth in the measured strain means that there has been a crack, most likely attributable to the release of the prestressing force, before the loading. A sudden increase in crack width indicates a new crack. An example of the former and latter behaviour are illustrated e.g. by transducers 35 and 34, respectively, see Fig. 49.





*Fig. 43. Strain measured by gauges 1–5.*







*Fig. 45. Strain measured by gauges 11–15. Fig. 46. Strain measured by gauges 16–20.* 





*Fig. 47. Strain measured by gauges 21–25. Fig. 48. Strain measured by gauges 26–30.*







## **APPENDIX A: PHOTOGRAPHS**



Fig. 1. Overview of floor test.



Fig. 2. Longitudinal view of floor test.



Fig. 3. End beam.



Fig. 4. Failure at stage 1.



Fig. 5. Failure at stage 3. Side view.



Fig. 6. Failure at stage 3 seen from above.



Fig. 7. Failure at stage 3 seen from above after removal of loading equipment.



Fig. 8. Concrete in hollow cores. Note the proper filling.



Fig. 9. Filling of outermost hollow core. Note the perfect filling on the top.



Fig. 10. End of slab unit no 3 after removal. Note the cracking of the shear keys.



Fig. 11. Cracking of joint concrete along middle beam. Note the cracking of the shear keys.



Fig. 12. Concrete filling between hollow core slab and ledger of middle beam. Note the perfect penetrationof the concrete under the end of the slab.



Fig. 13. Cracking of joint concrete along edge of middle beam.



Fig. 14. Cracking of tie beam at end of slab unit no 5 at stage 3.



Fig. 15. Cracking pattern of slab unit no 1 in reference test.



Fig. 16. Failure pattern of slab unit no 5 in reference test. The strand buckled when lifting the slab unit after the test.



Fig. 17. Failure pattern of slab unit no 7 in reference test.



Fig. 18. Failure pattern of slab unit no 8 in reference test.





















*Fig. 24. Stage 1. Support reaction measured below South end of the middle beam vs. load on half floor =*  $2(P_1 + P_2)$ *.* 


















*Fig. 30. Deflection on line IV, middle beam.* 













*is 0,03%. The length of the broken line corresponds to the length of the visible crack.*





## **APPENDIX A: PHOTOGRAPHS**



Fig. 1. Loading arrangement in floor test.



Fig. 2. Inductive transducer measuring differential horizontal displacement between top surface of beam and hollow core slab.



Fig. 3. Failure at stage 1. Side view.



Fig. 4. Failure at stage 1 seen from above.



Fig. 5. Failure at stage 1. The narrow crack above the failure crack appeared first. Its growth could be followed visually until failure.



Fig. 6. Cracking of the joint concrete along the beam at stage 2.



Fig. 7. Failure at stage 2 seen from above after removal of loading equipment.

## VTT.S.WQ.400.1992



Fig. 8. Failure at stage 2 seen from above after removal of loading equipment.



Fig. 9. Failure at stage 2 seen from above after removal of loading equipment.



Fig. 10. Failure at stage 2 seen from above after removal of loading equipment.



Fig. 11. Failure at stage 2 seen from below.



Fig. 12. Failure pattern of slab unit no 4 in reference test.



Fig. 13. Failure pattern of slab unit no 8 in reference test.



















*Fig. 20. Ratio of measured support reaction (below South end of the middle beam) to load on half floor.* 



*Fig. 21. A part of the previous figure in a large scale.* 

The shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

 $V_{obs} = V_{q,sl} + V_{q,ic} + V_{eq} + V_p$ 

where *Vg,sl*, *Vg,jc*, *Veq* and *Vp* are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of topping concrete, weight of loading equipment and actuator forces *Pi*, respectively.

The shear force at failure is calculated assuming that the slabs behave as simply supported beams. For  $V_{eq}$  and  $V_P$  this means that  $V_{eq} = 0.756 \times (8 \times 1.4 + 8 \times 1.8)/8 = 2.4$  kN and  $V_p = 0.756 \times (4 \times P_1 + 4 \times P_2 + 8 \times P_3)/8$ .  $V_{g,c}$  is calculated from the nominal geometry of the joints and measured density of the concrete, other components of the shear force are calculated from measured loads and weights. The values for the components of the shear force are given in Table on the next page.







*Fig. 24. Deflection measured by transducers 15–19.* 



*Fig. 25. Deflection measured by transducers 20–24.* 
















*Fig. 41. Slippage of outermost strands measured by transducers 7 and 8.* 



*Fig. 42. A part of the previous figure in a larger scale.* 

*Table. Reference tests. Span of slab, shear force V<sub>g</sub> at support due to the self weight of the slab, actuator force P at failure, weight of loading equipment Peq, total shear force*   $V_{obs}$  at failure and total shear force  $v_{obs}$  per unit width.





## **APPENDIX A: PHOTOGRAPHS**



Fig. 1. Overview of test arrangement in floor test.



Fig. 2. Longitudinal view of loading equipment. Actuators of type 2 on the right and on the left. Actuators of type 3 in the middle.



Fig. 3. Actuators of type 3. Note the white teflon sheets between the load distributing beams and above the actuators.



Fig. 4. View of end beam.



Fig. 5. Equipment for measuring transverse displacement of slab with reference to beam.



Fig. 6. Flexural cracking of slab unit no 4.



Fig. 7. Shear cracking of slab unit no. 4. Note also the growth of the flexural crack.



Fig. 8. Cracking pattern of slab unit no 4 before failure.



Fig. 9. Failure of slab unit no 4.



Fig. 10. Failure of slab unit no 4.



Fig. 11. Failure of slab unit no. 4 seen from above.



Fig. 12. Failure of slab unit no 4 seen from above.



Fig. 13. Failure of slab unit no 4 seen from above.



Fig. 14. Failure of slab unit no 4 seen from below after removal of loading.



Fig. 15. Failure of slab unit no 8.



Fig. 16. Failure of slab unit no 8. Note also the cracking of the ledge of the beam.



Fig. 17. Cracking of slab unit no 1.



Fig. 18. Longitudinal and transverse cracking of slab unit no 3 seen from below.



Fig. 19. Void filling at end of slab unit no 8 (upside down).



Fig. 20. Void filling at end of slab unit no 8 (upside down). Note that the concrete has filled the void completely.



Fig. 21. Cracking of joint concrete along middle beam after removal of loading.



Fig. 22. Cracking of end 2 of middle beam. The inductive transducers no 62 and 63 were attached to the steel plates which moved with reference to the beam when the corners of the beam cracked.



Fig. 23. Cracking of end 1 of middle beam.



Fig. 24. Reference test R1. Failure pattern.



Fig. 25. Reference test R1. Failure pattern.



Fig. 26. Reference test R1 (photographed after the failure). The width of the diagonal crack in the figure was several millimetres before the failure took place to the left of the diagonal crack (see Figs 24 and 25).



Fig. 27. Reference test R2. Failure pattern.



Fig. 28. Reference test R2. Failure pattern.























*Fig. 21. Ratio of measured support reaction (below South end of the middle beam) to load on half floor =*  $2(P_1 + P_2)$ *.* 

The shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

 $V_{obs} = V_{q,s} + V_{g,ic} + V_{g,top} + V_{eq} + V_p$ 

where  $V_{q,s}$ ,  $V_{q,i}$ ,  $V_{q,t}$ ,  $V_{eq}$  and  $V_p$  are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of topping concrete, weight of loading equipment and actuator forces *Pi*, respectively.

The shear force due to the the self-weight of the structure is calculated assuming that the slabs behave as simply supported beams.  $V_{eq}$  and  $V_P$  are calculated using the measured relationship between the support reaction of the beam and the loads. This means that  $V_{eq} = 0.883 \times P_{eq}$  and  $V_p = 0.883 \times (P_1 + P_2)/2$ .  $V_{g,jc}$  and  $V_{g,top}$  are calculated from the nominal geometry of the joints, nominal thickness 60 mm of the topping and measured density of the concrete, other components of the shear force are calculated from measured loads and weights. The values for the components of the shear force are given in Table below.

*Table. Components of shear resistance due to different loads.* 



The observed shear resistance  $V_{obs}$  = 140,3 kN (shear force at support) is obtained for one slab unit with width = 1,2 m. The shear force per unit width is *vobs =* **116,9 kN/m**


















## **APPENDIX A: PHOTOGRAPHS**



Fig 1. The prestressed concrete middle beam on the supports.



Fig. 2. A hollow core slab unit supported on the middle beam.



Fig. 3. Loading and measurement arrangement.



Fig. 4. Loading arrangement.



Fig. 5. Measurements for the displacement difference between the middle beam and the end of a slab unit and that one between the edges of a slab unit on the surface of the concrete topping.



Fig. 6. Measurement for the displacement difference between the edges of a slab unit on the bottom of the slab.



Fig. 7. Measurement for the displacement difference between the end of the middle beam and the edge of a slab unit.



Fig. 8. A crack in the middle of the concrete tie beam, between the slab unit no 2  $and 3.$ 



Fig. 9. A crack in the middle of the concrete tie beam, between the slab units no 6 and 7.



Fig. 10. The cracks in the longitudinal edge of the slab unit no 1, near the middle beam, at failure.



Fig. 11. The cracks in the longitudinal edge of the slab unit no 5, near the middle beam, at failure.



Fig. 12. The cracks in the longitudinal edge of the slab unit no 4, near the middle beam, at failure.



Fig. 13. The cracks in the longitudinal edge of the slab unit no  $8$ , near the middle beam, at failure.



Fig. 14. The cracking of the concrete topping along the joint between the middle beam and the ends of the slab units no  $1 - 2$  and no  $5 - 6$ .



Fig. 15. The cracking of the concrete topping along the joint between the middle beam and the ends of the slab units no  $1 - 3$  and no  $6 - 7$ .



Fig. 16. The cracking of the concrete topping along the joint between the middle beam and the ends of the slab units no  $3 - 4$  and no  $7 - 8$ .



Fig. 17. The cracking of the concrete topping and the tie beam between the slab units no 2 and 3.



Fig. 18. The cracking of the concrete topping and the tie beam between the slab units no 6 and 7.



Fig. 19. The failure of the end 1 of the slab unit no 9 in the reference loading test.



Fig. 20. The failure of the end 2 of the slab unit no 9 in the reference loading test.



Fig. 21. The middle beam after the loading test, on the side of the slab units no 1  $-4.$ 



Fig. 22. The middle beam after the loading test, or the side of the slab units no 5  $-8.$ 



























*Fig. 22. A part of the previous figure in a large scale. The point corresponding to the highest support reaction has been indicated by an arrow.* 

The observed shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

 $V_{obs} = V_{g,sl} + V_{g,ic} + V_{eq} + V_p$ 

where *Vg,sl*, *Vg,jc*, *Veq* and *Vp* are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of loading equipment and actuator forces  $P_1$ , and  $P_2$ , respectively.

It is concluded that the maximum support reaction due to the imposed load on the failed slabs has been  $V_p = 0.874$  x (actuator loads on half floor) /

 $4 = 0.874x(167.5 + 171.2)$  /2 = 148.0 kN. In the same way, the support reaction due to the weight of the loading equipment has been  $0.874x(1,2+5,6)/2 = 2.97$  kN.  $V_{q,c}$  is calculated from the nominal geometry of the joints and measured density of the grout. When calculating *Vg,sl*, the measured weight of the slabs is used. The values of the shear force components are given in Table 1 below.

*Table 1. Components of shear resistance due to different loads.* 



The observed shear resistance  $V_{obs}$  = 163,8 kN (shear force at support) is obtained for one slab unit with width = 1,2 m. The shear force per unit width is  $v_{obs}$  = 136,5 kN/m.


















# **APPENDIX A: PHOTOGRAPHS**



Fig. 1. The prestressed concrete middle beam on the supports.



Fig. 2. Cracking of the middle beam before the loading test.



Fig. 3. The dowel reinforcement and top surface of the middle beam.



Fig. 4. The loading and measurement arrangement.



Fig. 5. Hydraulic jacks and spreader beams.



Fig. 6. Devices to measure the displacement differences between the middle beam and the ends of the slab units and between the edges of the slab units or between the corresponding points at the middle beam.



Fig. 7. The cracks in the longitudinal edge of the slab unit no  $1$ , near the middle beam, at failure.



Fig. 8. The cracks in the longitudinal edge of the slab unit no 5, near the middle beam, at failure.



Fig. 9. The cracks in the longitudinal edge of the slab unit no 8, near the middle beam, at failure.



Fig. 10. The cracks in the longitudinal edge of the slab unit no 4, near the middle beam, at failure.



Fig. 11. Cracking of the joint between the cast in situ part of the middle beam and the ends of the slab units.



Fig. 12. The middle beam after the loading test, on the edge of the slab units no 1  $-4.$ 



Fig. 13. The middle beam after the loading test, on the edge of the slab units no 5  $-8.$ 



Fig. 14. The failure of the end 1 of the slab unit no 9 in the reference loading test.



Fig. 15. The failure of the end 2 of the slab unit no 9 in the reference loading test.



Fig. 16. The failure of the end 1 of the slab unit no 10 in the reference loading test.



Fig. 17. The failure of the end 2 of the slab unit no 10 in the reference loading test.



















The weight of loading equipment per actuator was 1,2 kN and 5,6 kN for actuators *P1* and *P2*, respectively. Consequently, the imposed load per slab was

 $F_1 = P_1 + 1.2$  kN for slabs 2, 3, 6 and 7  $F_2 = P_2 + 5.6$  kN for slabs 1, 4, 5 and 8

*The weight of the loading equipment below actuator loads P3 was 0,5 kN and* 

 $F_3 = P_3 + 0.5$  kN on the middle beam.

The bending moment between the supports of the middle beam followed closely the elastic bending moment distribution until  $P_1 = P_2 = 160$  kN,  $P_3 = 450$  kN. Thereafter  $P_3$ was kept constant. The bending moment in the span was roughly equal but opposite to that at supports, see Fig. 25.



*Fig. 25. Bending moment diagram of middle beam between supports at failure.* 







*actuator loads on half floor.* 



*Fig. 30. A part of the previous figure in a large scale.* 

The observed shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

 $V_{obs} = V_{a.si} + V_{a_ic} + V_{eq} + V_p$ 

where *Vg,sl*, *Vg,jc*, *Veq* and *Vp* are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of loading equipment and actuator forces  $P_1$ , and  $P_2$ , respectively.

It is concluded that the maximum support reaction due to the imposed load on the failed slabs has been  $V_p = 0.88$  x (actuator loads on half floor) /

 $4 = 0,88$  x(199,7 + 200,5) /2 = 176,09 kN. In the same way, the support reaction due to the weight of the loading equipment has been  $0,88x(1,2+5,6)/2 = 2,99$  kN.  $V_{q,c}$  is calculated from the nominal geometry of the joints and measured density of the grout. When calculating *Vg,sl*, the measured weight of the slabs is used. The values of the shear force components are given in Table 1 below.

*Table 1. Components of shear resistance due to different loads.* 



The observed shear resistance  $V_{obs}$  = 191,4 kN (shear force at support) is obtained for one slab unit with width = 1,2 m. The shear force per unit width is  $v_{obs}$  = 159,5 kN/m.







*Fig. 33. Deflection on line III, middle beam.* 



*Fig. 34. Deflection on line IV.* 













## **APPENDIX A: PHOTOGRAPHS**



Fig. 1. Overview of test arrangements in floor test.



Fig. 2. Skew ends of slab units at middle beam.



Fig. 3. Hydraulic actuator on end of middle beam.



Fig. 4. Support above end of end beam.



Fig. 5. Equipment for measuring transverse displacement of slab relative to middle beam.



Fig. 6. Equipment for measuring transverse average strain of hollow core units and middle beam.



Fig. 7. Shear cracking of slab unit no 1. Note also the flexural cracks in the beam.



Fig. 8. Cracking pattern of slab unit no 1 seen from above.



Fig. 9. Failure of slab unit no 4.



Fig. 10. Failure of slab units nos 1 - 4 seen from below.


Fig. 11. Cracks in the middle beam and along the joint between the slab ends and the beam.



Fig. 12. Reference test. Failure of slab unit no 9, end 1, edge 1.

## VTT.PC.InvT\_Cont.265.1994



Fig. 13. Reference test. Failure of slab unit no 9, end 1, edge 2.



Fig. 14. Reference test. Failure of slab unit no 9, end 2, edge 1.



Fig. 15. Reference test. Failure of slab unit no 9, end 2, edge 2.





























TUT.CR.MEK.265.1994









Deflections *Table 2. Support reaction below South end of MEK beam and deflection measured by transducers 13–15, both due to installation of hollow core slabs, grouting and loading equipment.* 















## TUT.CR.MEK.265.1994















## **2.7**  Loading The loads *P*, see Fig. 11, were generated by 6 identical hydraulic actuators, each arrangements connected to the same hydraulic pressure. The actuator loads were spreaded with the aid of 6 primary, 12 secondary and 24 tertiary spreader beams to two transverse line loads on the slabs as shown in Figs 11–13. The reaction forces of the actuators were carried by a temporary steel frame which was fixed to the floor of the hall by tension bars. Four holes were drilled through the test floor for these bars. The position of the tension bars is shown in Fig. 11. After the test it came out that the holes had no effect on the failure mechanism. The tertiary spreader beams on the top of the floor were slightly shorter than 0,6 m. The friction between the teriary and secondary beams was eliminated by roller bearings and that between the secondary and primary spreader beams by teflon plates. There was gypsum mortar between the tertiary spreader beams and the top surface of the floor. 1200<sup>290</sup> 1200  $\otimes$  Hole through floor Hydraulic actuator  $\overline{\mathbf{A}}$ North P h  $\mathbf{\overline{12}}$  $\epsilon$  $\overline{\mathbb{R}}$ P கி  $(11)$  $\left(5\right)$  $\overline{\mathsf{h}}$ P  $\overline{10}$ 4 7200  $\overline{\Pi}$ P h 9  $\left(3\right)$ P  $\overline{\mathbf{8}}$  $\left( 2\right)$  $\overline{\Pi}$ h P 7  $\boxed{1}$  $\Box$ 6000 6000 South 12290 A Det A **Teflon**  $\mathsf{P}$   $\downarrow$  P  $\downarrow$  P  $\downarrow$  P sheets rt<del>n</del> 7200  $A = A$ *Fig. 11. Loading arrangements.*


























*Fig. 42. Net mid-point deflection of slabs 13 and 14. Rigid body motion (= settlement of supports) has been eliminated*.

The failure modes and failure loads are given in Table 2. The measured self-weight of the slabs = 4,33 kN/m has been used when calculating the shear resistance.

*Table 2. Span L, ultimate load Pu, shear force due to self weight Vg, shear force due to imposed load*  $V_P$ *, ultimate shear force*  $V_u$  and failure mode in reference tests. The weight *of the loading equipment = 1,0 kN is included in Pu.* 





## **APPENDIX A: PHOTOGRAPHS**



Fig. 1. Assembling specimen.



Fig. 2. Overview of test arrangements.



Fig. 3. Hydraulic actuator between the loading frame and a tertiary spreader beam. Note the teflon sheets.



Fig. 4. Primary, secondary and tertiary spreader beam. Note the teflon sheets and the movable bar.



Fig. 5. Equipment for measuring transverse displacement of slabs and joint concrete relative to the middle beam.



Fig. 6. The same as above.



Fig. 7. Flexural cracking of the middle beam before loading.



Fig. 8. Failure pattern of slab unit No. 7.



Fig. 9. Failure pattern of slab unit No. 7 seen from above.



Fig. 10. Cracking pattern of slab unit No. 1 after failure of slab unit No. 7.



Fig. 11. Cracking pattern of slab unit No. 12 after failure of slab unit No. 7.



Fig. 12. Cracking pattern of slab unit No. 6 after failure of slab unit No. 7.



Fig. 13. Cracking pattern at end of slab unit No. 1.



Fig. 14. Cracks between the slab ends and joint concrete.



Fig. 15. Cracks between the slab ends and joint concrete.



Fig. 16. Cracking along joint between adjacent slab units.



Fig. 17. Cracking of slab unit No. 6.



Fig. 18. Typical cracking of concrete infill in the cores of slab unit No. 5.



Fig. 19. Middle beam after removal of slabs units. Side supporting slab units No.  $5$  and  $6$ .



Fig. 20. Middle beam after removal of slab units. Side supporting slab units  $No$ .  $1$  and  $2$ .



Fig. 21. Middle beam after removal of slab units. Side supporting slab units No.  $7 - 12.$ 



Fig. 22. Concrete infill below the slab ends. Note that the grout has properly filled the space. Note also the pores due to the air bubbles.





















## VTT.CP.LBL.320.1998







*Fig. 23. Ratio of measured support reaction of the middle beam (R<sub>p,obs</sub>) to theoretical support reaction (* $R_{p,th}$ *) vs. actuator force*  $P_{a1}$ *. Only actuator loads*  $P_{a1}$  *and*  $P_{a2}$  *are taken into account in the support reaction.* 

Assuming simply supported slabs and calculating the support reaction of the actuator loads from equilibrium of forces, gives support reaction which is 83,7% of the actuator loads. On the other hand, just before the failure, the measured support reaction under the North end of the middle beam was 81,68% of the loads on half floor. Using this relationship for the weight of loading equipment, and assuming that the weight of the slabs and jointing concrete was distributed to both ends of the slab units as if the slabs were simply supported beams, the shear resistance of one slab end (support reaction of slab end at failure) due to different load components can be calculated as shown below.

*Table. Components of shear resistance due to different loads.* 



The shear resistance of one slab end due to imposed load

 $V_{obs,imp} = V_p + V_{eq} = 139,8 \text{ kN} + 2,78 \text{ kN} = 142,6 \text{ kN}$ 

and the total shear resistance

 $V_{obs} = V_{obs, imp} + V_{g, sl} + V_{g, iso} = 142,6$  kN + 18,5 kN + 0,8 kN = 161,9 kN

are obtained.

The observed shear resistance  $V_{obs}$  = 161,9 kN (shear force at support) is obtained for one slab unit with width = 1,2 m. The shear force per unit width is  $v_{obs}$  = 134,9 kN/m.












*Fig. 40. Actuator force – time relationship. R1 : Slab 9; R2:Slab 10.* 











## **APPENDIX A: STEEL COMPONENT OF LBL BEAM**



*Fig. 1. Steel component of LBL beam. Elevation (lattice girders) and plan (bottom plate). See Fig. 2 for sections A, B and C.*



*Fig. 2. Sections A, B and C, see Fig. 1.*



*Fig. 3. Splicing of lattice girders.*



*Fig. 4. Bottom flange and position of lattice girders.*





*Fig. 5. Design of lattice girders.*

### **APPENDIX B: PHOTOGRAPHS**





*Fig. 1. Overview. Fig. 2. Loading equipment.*





*Fig. 3. Arrangements at end beams. Fig. 4. Transducers at the end of middle beam.*





*Fig. 5. Failure pattern of slab unit 5. Fig. 6. Detail of slab unit 5 after failure.*



*Fig. 7. Slab unit 5 seen from above after failure. Fig. 8. Failure pattern of slab unit 8.*





*Fig. 9. Cracking pattern of slab unit 1 after failure of slab units 5–8.* 



*Fig. 11. Cracking pattern of slab unit 4 after failure of slab units 5–8.*



*Fig. 10. Detail of slab unit 1. Note the transverse crack in the soffit.*



*Fig. 12. Failure pattern of slab units 5–8 seen from above.*



*Fig. 13. Failure pattern of slab units 5–8 seen from below.* 



*Fig. 15. Edge of middle beam after removing slab units 1–4.* 



*Fig. 17. Detail of middle beam after removing slab units.*



*Fig. 14. Failure pattern of slab units 5–7 seen from below.*



*Fig. 16. Edge of middle beam after removing slab units 5–8.*



*Fig. 18. Failure pattern of slab unit 9 in reference test.*

#### VTT.CP.LBL.320.1998



*Fig. 19. Failure pattern of slab unit 9 in reference test.*



*Fig. 20. Failure pattern of slab unit 10 in reference test.* 



*Fig. 21. Failure pattern of slab unit 10 in reference test.*











#### VTT.CR.Delta.400.1999













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Assuming simply supported slabs and calculating the support reaction of the actuator loads from equilibrium of forces gives a support reaction which is 86,1% of the actuator loads. On the other hand, just before the failure, the measured support reaction under end 2 of the Delta beam was 82,9% of the loads on half floor. Using this relationship also for the weight of loading equipment, and assuming that the weight of the slabs and cast-in-situ concrete was distributed to both ends of the slab units as if the slabs were simply supported beams, the shear resistance of one slab end (support reaction of slab end at failure) due to different load components can be calculated as shown in Table 2.



*Table 2. Components of shear resistance due to different loads.* 

The shear resistance of one slab end due to imposed load

$$
V_{u,imp} = V_p + V_{eq} = 195,1 \text{ kN} + 2,8 \text{ kN} = 197,9 \text{ kN}
$$

and the total shear resistance

 $V_{\mu} = V_{\mu \text{ imp}} + V_{\text{gas}} + V_{\text{g}} = 197.9 \text{ kN} + 22.7 \text{ kN} + 1.4 \text{ kN} = 222.0 \text{ kN}$ 

are obtained.

The strong deviation of the support reaction from the simply supported behaviour of the slab units at  $P_{a1}$  < 100 kN cannot be explained by the negative bending moment carried by the tie reinforcement penetrating the Delta beam. The bending moment corresponding to the yield stress 500 MPa of the tie reinforcement is of the order of 37 kNm per floor and 37/4 = 9,3 kNm per slab unit. This increases the support reaction of one slab unit at the Delta beam by 1,1 kN which is far too small to explain the behaviour. It is more likely that the extra support moment is due to the joint concrete. The tie reinforcement obviously helps in mobilizing vertical friction, dowel action and aggregate interlocking along the inclined webs of the Delta beam, particularly in the web holes. With increasing crack width along the Delta beam these effects fade out.

At *Pa1* = 200 kN diagonal shear cracks at the ends of slab units 1 and 5 started to change the load-carrying mechanism of these slab units. The loads were more and more transferred to the neighbouring slab units and less directly to the beam. As a result, the support reactions of the Delta beam became different in such a way that the reaction force at the North end was smaller than that at the opposite end. This effect can be seen in Fig. 25 when *Pa1* is greater than 200 kN.









displacement



*Fig. 37. Northern end of middle beam. Differential displacement between edge of slab and middle beam. A negative value means that the slab is moving towards the end of the beam.*



*Fig. 38. Southern end of middle beam. Differential displacement between edge of slab and middle beam. A negative value means that the slab is moving towards the end of the beam.*



*Fig. 39. Shear displacement = differential displacement at upper edge – differential displacement at lower edge of slab.* 

#### **10.5 Strain**





*Fig. 41. Strain measured by gauges 60 and 61 parallel to Delta beam.*

#### VTT.CR.Delta.400.1999





# **APPENDIX A: PHOTOGRAPHS**



*Fig. 1. Delta-beam (middle beam in floor test).* 



*Fig. 2. Detail of Delta-beam.*


*Fig. 3. Overview of test arrangements.* 



*Fig. 4. Loading arrangements.* 

## VTT.CR.Delta.400.1999



*Fig. 5. Arrangements at support of middle beam.* 



*Fig. 6. Measuring equipment on slab units 2, 3, 6 and 7.* 



*Fig. 7. Arrangements at support of end beam.* 



*Fig. 8. Failure pattern of slab unit 5.* 



*Fig. 9. Failure pattern of slab unit 1.* 



*Fig. 10. Failure pattern of slab unit 4.* 



*Fig. 11. Failure pattern of slab unit 8.* 



*Fig. 12. Cracking pattern of tie beam between slab units 2 and 3 at failure of the floor.* 



*Fig. 13. Cracking pattern of tie beam at end of slab units 6 and 7 at failure of the floor.* 



*Fig. 14. Deformation of ledge of Delta-beam under slab units 5–8 after failure of the floor.* 



*Fig. 15. Deformation of ledge of Delta-beam under slab units 5–8 after failure of the floor.* 



*Fig. 16. Deformation of ledge of Delta-beam under slab unit 5 after failure of the floor.* 



*Fig. 17. Top surface of the floor after removal of loads.* 



*Fig. 18. Top surface of slab unit 5 after failure.* 



*Fig. 19. Top surface of slab unit 6 after failure.* 



*Fig. 20. Top surface of slab unit 7 after failure.* 



*Fig. 21. Top surface of slab unit 8 after failure.* 



*Fig. 22. Top surface of slab unit 1 after failure.* 



*Fig. 23. Cracks along middle beam.* 



*Fig. 24. Cracks along middle beam.* 



*Fig. 25. Joint concrete between slab unit 5–8 and midde beam after removal of slab units.* 



*Fig. 26. Detail of the joint concrete after failure.* 



*Fig. 27. Web and deformed ledge of middle beam after removal of slab units and joint concrete. The tie bars penetrating the beam have been flame-cut after the test.* 



*Fig. 28. Detail of middle beam after failure.* 



*Fig. 29. Reference test R9/1. Failure pattern.* 



*Fig. 30. Reference test R9/1. Failure pattern.* 



*Fig. 31. Reference test R9/2. Failure pattern.* 



*Fig. 32. Reference test R9/2. Failure pattern.* 

































The shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

$$
V_{obs} = V_{g, sl} + V_{g, ic} + V_{eq} + V_a
$$

where *Vg,sl*, *Vg,jc*, *Veq* and *Va* are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of loading equipment and actuator forces *Pai*, respectively. All components of the shear force are calculated assuming that the slabs behave as simply supported beams. For  $V_{eq}$  and  $V_a$  this means that  $V_{eq} = 0.8677 \times P_{eq}$  and  $V_a =$ 0,8677x(*Pa1* + *Pa2*)/2. *Vg,jc* is calculated from the nominal geometry of the joints and density of the concrete, other components of the shear force are calculated from measured loads and weights. The values for the components of the shear force are given in Table below.

*Table. Components of shear resistance due to different loads.* 



The observed shear resistance  $V_{obs}$  = 127,5 kN (shear force at support) is obtained for one slab unit with width = 1,2 m. The shear force per unit width is *vobs =* **106,2 kN/m**



## **10 Measured displacements**

In the following figures,  $V_a$  stands for the shear force of one slab end due to imposed actuator loads, calculated assuming simply supported slabs. Note that the last three points on each curve represent the post failure situation for which the real shear force has been lower than that shown in the figures. This note is based on the measured support reaction, see Fig. 25.b.

**10.1** 

**Deflections** 





*Fig. 34. Deflection on line I along western end beam.* 



*Fig. 36. Deflection on line III close to the line load, slabs 1–4.*



*Fig. 38. Deflection on line V close to the line load, slabs 5–8.* 

*Fig. 35. Deflection on line II in the middle of slabs 1–4.* 



*Fig. 37. Deflection on line IV along the middle beam.* 



*Fig. 39. Deflection on line VI in the middle of slabs 5–8.* 





## VTT.CP.Super.320.2002




### **APPENDIX A: DETAILS OF SUPER BEAM**







# **APPENDIX B: PHOTOGRAPHS**



*Fig. 1. Tie reinforcement at the edge of the floor.* Fig. 2. Overview on arrangements.







*Fig. 3. Loading arrangements. Fig. 4. Transducers measuring average strain in beam's direction.*





*Fig. 7. Arrangements for line loads. Fig. 8. Failure of slab 5.* 





*Fig. 5. Arrangements at end beam. Fig. 6. Transducers measuring sliding of slabs along middle beam.* 





*Fig. 9. Failure of slab 1. Fig. 10. Diagonal crack in slab 8 after failure.*





*Fig. 13. Wide crack along the western edge of middle beam next to slab 2.* 



*Fig. 11. Failure of slab 4. Fig. 12. Vertical cracking of end beam between slabs 6 and 7.* 



*Fig. 14. Failure cracks in slab 2.*





*Fig. 15. Cracks in slab 4 after failure. Fig. 16. Cracks in slabs 2–4 after failure.*





*Fig. 19. Soffit of slabs 3 and 4 after failure. Fig. 20. Soffit of slabs 1–2 after failure.*



*Fig. 17. Cracks in slab 5 after failure. Fig. 18. Cracks in slab 1 after failure.*





*Fig. 21. Failed ends of slabs 3–4 after failure.* 



*Fig. 23. Eastern side of middle beam after demolition. Fig. 24. Western side of middle beam after* 



*Fig. 22. Western side of middle beam. Note the bond failure along the vertical interface of the castin-situ concrete and the precast beam as well as the intact core fillings.*



*demolition.*



*Fig. 25. Intact core fillings after failure. Note the geometric imperfections at the end.* 





*Fig. 26. Web shear failure in reference test R9/2.*



*Fig. 27. Web shear failure in reference test R9/2. Fig. 28. Flexural shear failure in reference test R9/1.*



*Fig. 29. Flexural shear failure in reference test R9/1.*





























 $V_{obs} = V_{g,s} + V_{g,jc} + V_{eq} + V_P$ 









*Fig. 32. Longitudinal concrete strain in LB beam measured by gauges 47, 48 and 49. The strain measured by gauge 46 is not shown because it was clearly erroneous.* 





# **APPENDIX A: PHOTOGRAPHS**



*Fig. 1. Loading arrangements.* 



*Fig. 2. Equipment for measuring average strain in hollow core slab.* 



*Fig. 3. A step between LB beam and slab 4.* 



*Fig. 4. Failure in slab 8.* 



*Fig. 5. Soffit after failure. Slab 6 in the front, slabs 7 and 8 in the rear.* 



*Fig. 6. Slab 8 after failure. The loose top part has been removed.* 



*Fig. 7. Slab 8 after failure. All loose concrete material has been removed.* 



*Fig. 8. Failure mode in reference test.* 
























#### **Observations after failure**

When slab 12 failed, the loads on it were transferred to slab 11 over the longitudinal joint. The strength of this joint and the elastic energy stored in the loading frame made the floor fail in a complicated manner illustrated in Fig. 33 and in App. A, Figs 26–33. Despite the complexity of the crack pattern after the test, the origin of the failure was the shear crack in slab 12 next to the middle beam.

#### About core filling

After the test, the concrete filling of the slab ends next to the middle beam was investigated. In all hollow cores there was an empty space above the infill in the upper outer corner as shown in App. A, Figs 48–50. This was observed first after the end of slab 12 and the cast-in-situ concrete around it was broken during demolition. Fig. 24 shows the average geometry of the core infill for slabs 1 and 12. To illustrate the scatter, the geometry of the core infill for the individual cores is shown with dashed lines for slab 1.



#### Observations on support conditions of slabs

The soffit of the slab units was not in complete contact with the middle beam when the slabs were installed and grouted, see Fig. 27. There were two reasons for this phenomenon. Firstly, the middle beam was stiffer than the end beams and had a precamber of 4 mm while the end beams were straight and deflected downwards due to their self weight. Due to these effects the slab ends were laying on non-parallel supports. Secondly, the soffit of the slabs was not completely planar but slightly curved downwards in transverse direction. Fig. 28 illustrates the typical joint between the outermost slabs and the ledge of the WQ beam. This gap was partly filled with the cement paste, and where wide enough, was also filled with the grout including aggregate. This is shown in App. A, Figs 53–59. At the support of the beam, the source of the grout below the slab was either the edge grouting as shown in Fig. 28 and App. A, Figs 41 and 44–47, or end grouting.

After the test, the maximum gap width  $\delta_{\text{max}}$  was measured for the outermost slabs where possible. The results are given in the caption of Fig. 29.





*Fig. 27. Typical gap between slab and beam flange.*  $\delta_{\text{max}} = 1.3$  mm, 3,8 mm and *5,5 mm for slabs 1, 6 and 7, respectively. For slab 12 the gap could not be measured after the failure.* 

*Fig. 28. Concrete cast outside the outermost edges of slabs intruded below the slab to some extent.* 

Fig. 29 shows the horizontal dimensions of a relatively thick grouting below the corners of the slab. These were measured using a steel wire which was 1 mm thick. Slab 1 was not checked because the wire was too thick for the gap. Slab 12 could not be measured because the concrete broken in the failure had filled the gap.

A direct contact between the soffit of the slab end and the ledge of the beam or grout on the ledge represents a favourable support condition. In this test also other mechanisms to transmit the support reaction of the slab to the beam may have been present.

The slab units were saw-cut but there was 10 mm deep zone at the bottom of the slab cross-section, which was not sawn but broken, see App. A, Fig. 52. The rough surface of this zone could work as a dowel, see Fig. 30. Even more important may have been the fact that the reinforced cast-in-situ concrete formed a beam which with the aid of the concrete in the cores may have transmitted the loads from the slabs to the bottom flange of the beam. This load-carrying mechanism may have been effective enough to transmit the loads even without any contact between the flange of the beam and the precast slab unit as shown in Fig. 31.























# **APPENDIX A: PHOTOGRAPHS**



*Fig. 1. WQ beam.*



*Fig. 2. Initial crack in slab 1.*



*Fig. 3. Initial cracks in slab 2.*



*Fig. 4. Initial crack in slab 3.*

## VTT.PC.InvT.500.2006



*Fig. 5. Initial crack in slab 4.* 



*Fig. 6. Initial cracks in slab 5.*



*Fig. 7. Initial crack in slab 7.*



*Fig. 8. Initial crack in slab 8.*

## VTT.PC.InvT.500.2006



*Fig. 9. Initial cracks in slab 9.*



*Fig. 10. Initial crack in slab 11.*



*Fig. 11. Slabs 1,2,6,7,8 and 12 in their final position.*



*Fig. 12. Slab 12 on WQ beam and a tie bar 20 mm.*



*Fig. 13. A short, bent tie bar, outer edge of slab 1.*



*Fig. 14. Support conditions above end beam.*



*Fig. 15. Initial bending crack in slab 3 at a distance of 1050 mm from slab end.*



*Fig. 16. Initial bending crack in slab 9 at a distance of 1350 mm from slab end.*

## VTT.PC.InvT.500.2006



*Fig. 17. Overview on test arrangements.*



*Fig. 18. View on the loading frame and spreader beams.*



*Fig. 19. Actuators above primary spreader beams.*



*Fig. 20. Arrangements between spreader beams. Note the white teflon sheets between the primary and secondary spreader beams.*



*Fig. 21. Three orange load cells below one support of WQ beam.*



*Fig. 22. North end of WQ beam before loading.*



*Fig. 23. North end of WQ beam before loading.*



*Fig. 24. Longitudinal crack in the soffit of slab 10 at*  $P_a = 160$  *kN. The cracking took place at*  $P_a =$ *109 kN.*



*Fig. 25. Inclined crack in slab 7 at Pa = 213 kN.*



*Fig. 26. Failure of slab 12 at Pa = 272 kN.*


*Fig. 27. Failure of slab 12 at Pa = 272 kN.*



*Fig. 28. Failure of slab 12 at Pa = 272 kN.*



*Fig. 29. Failure of slab 12 at Pa = 272 kN.*



*Fig. 30. Failure of slabs 11 and 12 at Pa = 272 kN.*



*Fig. 31. Failure of slabs 11 and 12 at Pa = 272 kN.*



*Fig. 32. Slabs 11 and 12 after removing the loading equipment.*



*Fig. 33. Slabs 11 and 12 after removing the loading equipment.* 



*Fig. 34. Slab 7 after test. Cracks in tie beam. The read line and capital A indicate an initial crack.*



*Fig. 35. Slab 8 after test. Cracks in tie beam. The read line and capital A indicate an initial crack. The nonuniform colour is due to a mortar treatment carried out after demolding.* 



*Fig. 36. Slab 9 after test. Cracks in tie beam.*



*Fig. 37. Slab 10 after test. Cracks in tie beam.*



*Fig. 38. Slab 11 after test. Cracks in tie beam.*



*Fig. 39. Slab 12 after test. Cracks in tie beam.*



*Fig. 40. Slab 1 after test.*



*Fig. 41. Slab 1 after test.*



*Fig. 42. Slab 6 after test.*



*Fig. 43. Slab 12 after test.*



*Fig. 44. Slab 1 after test.*



*Fig. 45. Slab 7 after test.*



*Fig. 46. Slab 7 after test.*



*Fig. 47. Slab 6 after test.*



*Fig. 48. Failure surface at end of slab 1. Note the incomplete filling of the cores.*



*Fig. 49. Concrete filling taken from one core of slab 12.*



*Fig. 50. Concrete filling in one core of slab 2. Note that the polystyrene plug is inclined due to the casting pressure. Consequently, the length of the filling at the bottom is greater than 400 mm.*



*Fig. 51. Failure surface of slabs 11 and 12.*



*Fig. 52. Rough surface at slab end below even, saw-cut surface.*



*Fig. 53. Changes in colour on the flange below slab 1 due to the concrete or cement paste intruding into the gap between the soffit of the slab and the steel flange. See also the vertical stripes along the vertical edge of the flange.*



*Fig. 54. Thin layers of grout as well as changes in colour on the flange below slab 1 due to the grout intruding into the gap between the soffit of the slab and the steel flange.*



*Fig. 55. Thin layers of grout as well as changes in colour on the flange below slab 1 due to the grout intruding into the gap between the soffit of the slab and the steel flange.*



*Fig. 56. Thin layers of grout as well as changes in colour on the flange below slab 1 due to the grout intruding into the gap between the soffit of the slab and the steel flange.*



*Fig. 57. A detail of grout below slab 6.*



*Fig. 58. Grout below slab 5.*



*Fig. 59. Steel flange below slab 7. No clear sign of grout can be seen below the slab and above the flange.*



*Fig. 60. Overview on arrangements in reference test.*



*Fig. 61. Loading arrangements in reference test.*



*Fig. 62. Failure pattern in reference test. South edge.* 



*Fig. 63. Failure pattern in reference test. North edge.* 












































# **APPENDIX A: PHOTOGRAPHS**



*Fig. 1. Failure mode in reference test R1.*



*Fig. 2. Failure mode in reference test R2.*



*Fig. 3. Installing slabs on PC beam.* 



*Fig. 4. Uneven surface of concrete beam due to air bubbles.*



*Fig. 5. Initial crack in slab 3.* 



*Fig. 6. Initial crack in slab 4.*



*Fig. 7. Initial crack in slab 9.*



*Fig. 8. Initial crack in slab 10.*



*Fig. 9. A short tie bar through beam at support.*



*Fig. 10. Initial crack in slab 3.*

# VTT.PC.InvT.500.2006



*Fig. 11. Initial crack in slab 12.*



*Fig. 12. Initial crack in slab 12.*



*Fig. 13. Overview on test arrangements.* 



*Fig. 14. Support arrangement at end beam.*

# VTT.PC.InvT.500.2006



*Fig. 15. Shear crack at Pa = 308 kN. The black line drawn 200 mm below the shear crack is a misprint which does not refer to a crack.* 



*Fig. 16. Shear crack in slab 7 at Pa = 353 kN.*



*Fig. 17. Failure in slab 1. Photographed after stage II. In stage I, the failure crack was the same but much thinner.* 



*Fig. 18. Failure mode in slab 1.*

# VTT.PC.InvT.500.2006



*Fig. 19. Failure mode in slab 1.* 



*Fig. 20. Cracks in soffit of slabs 4 and 5 after failure.*



*Fig. 21. Crack in soffit of slab 11 after failure.* 



*Fig. 22. Failure mode.*



*Fig. 23. Core filling in slab 1.* 



*Fig. 24. Grout at support after removal of slab. Note the perfect filling of the gap below the slab end.* 



*Fig. 25. Perfect filling of hollow core. Note the lack of bond between the cast-in-situ and precast concrete.* 



*Fig. 26. The only observed incomplete filling in hollow core.* 



*Fig. 27. Cast-in-situ concrete below slab end. Good bond with slab, weaker bond with beam.* 



*Fig. 28. Cast-in-situ concrete below slab end. Good bond with beam, weaker bond with slab.*



*Fig. 29. Vertical cracking at slab ends took place along the web ob the beam.*



*Fig. 30. Vertical cracking at slab ends took place along the web ob the beam.*




































Figs 30 and 31 illustrate the ratio of measured support reaction  $R_{p,obs}$  to the theoretical support reaction  $R_{p,th}$  calculated from six actuator loads assuming simply supported slabs. Thus  $R_{p,th}$  is equal to (9900–1450)/9900x6x $P_a$  = 0,8535x6x $P_a$ . Before failure the maximum difference is -0,59%, i.e.  $R_{p,th}$  is less than 1% smaller than the measured support reaction. The assumption of simply supported slabs is accurate enough to justify the calculation of the experimental shear resistance based on it.











*Fig. 34. Deflection on line III close to the line load, slabs 1–6.*





*Fig. 36. Deflection on line V close to the* 

*line load, slabs 7–12.* 



*Fig. 38. Deflection on line VII along end beam, slabs 7–12.* 

*Fig. 37. Deflection on line VI in the middle of slabs 7–12.* 

0 5 10 15 20 25 30 35 40 Deflection [mm]



*Fig. 39. Net deflection of midpoint of middle beam (35) and those of end beams (14, 56). Settlement of supports eliminated.* 







*Fig. 41. Differential displacement at top surface of floor measured by transducers 67, 69, 71, 73, 75 and 77.* 



*Fig. 42. Differential displacement at soffit of floor measured by transducers 68, 70, 72, 74, 76 and 78.*





*Fig. 43. Top fibre of floor. Average strain calculated from the differential displacements shown in Figs 41–42.* 



*Fig. 45 Bottom fibre of floor. Initial part of the previous figure.* 

*Fig. 44. Bottom fibre of floor. Average strain calculated from the differential displacements shown in Figs 41–42.*



*Fig. 46. Average strain of slabs 3, 4, 9 and 10 as well as that of the middle beam at estimated service load Pa = 160 kN*   $(V_p = 137$  kN).







*Fig. 54. Actuator force – time relationship.* 

In both reference tests flexural cracks were observed below the loads before the shear tension failure took place in the webs close to the support. No visible slippage of the strands was observed before the failure. The failure modes are illustrated in Fig. 56 and in App. A, Figs 38–41.

The time dependence of the load and measured load – deflection relationship are shown in Figs 55.



*Fig. 55. Vertical displecements measured by transducers 1–6. V<sub>P</sub> is the support reaction due to actuator forces Pa.* 





## **APPENDIX A: PHOTOGRAPHS**

Note: In Figs. 23–33 the cracks marked with red colour and letter A refer to initial cracks which existed before the onset of the loading.



*Fig. 1. Delta beam as installed.* 



*Fig. 2. Delta beam as installed.* 



*Fig. 3. Slab placed on Delta beam.* 



*Fig. 4. Tie reinforcement at support of beam.* 



*Fig. 5. End of middle beam (Delta beam) after grouting.* 



*Fig. 6. Overview on test arrangements.* 



*Fig. 7. Loading equipment.* 



*Fig. 8. Longitudinal view on the loading equipment.* 



*Fig. 9. Actuators on the primary spreader beam and below the temporary loading frame.* 



*Fig. 10. Arrangements at end beam.* 



*Fig. 11. Transducers at end of middle beam.* 



*Fig. 12. Transducer, fixed to the bottom flange of the middle beam, measuring sliding of slab along beam.* 



*Fig. 13. Bottom flange of middle beam supporting slabs.* 



*Fig. 14. Equipment for measuring average transverse strain of the soffit.* 



*Fig. 15. Initial crack in slab 3 close to end beam.* 



*Fig. 16. Shear cracks in slab 7 at Pa = 336 kN.* 



*Fig. 17. Shear crack in slab 1 at Pa = 337 kN.* 



*Fig. 18. Shear cracks in slab 1 after failure at Pa = 382 kN.* 



*Fig. 19. Shear cracks in slab 1 after removing the loading equipment.* 



*Fig. 20. Failure pattern on the top of slab 1 after removing the loading equipment and drilling the cores.* 



*Fig. 21. Slab 1 after removing slabs 2–6 and 8–12.* 



*Fig. 22. Perfect filling in a hollow core of slab 1.* 



*Fig. 23. Cast-in-situ concrete after removing the slabs. Note the grout layer between the slab and the flange of the beam.* 



*Fig. 24. Western end beam. Cracks in cast in-situ concrete at the end of slabs 1 and 2.* 



*Fig. 25. Western end beam. Cracks in cast in-situ concrete at the end of slabs 1 and 2.* 



*Fig. 26. Western end beam. Cracks in cast in-situ concrete at the end of slabs 2–4.* 



*Fig. 27. Western end beam. Cracks in cast in-situ concrete at the end of slabs 3–5.* 



*Fig. 28. Western end beam. Cracks in cast in-situ concrete at the end of slabs 4–6.* 



*Fig. 29. Western end beam. Cracks in cast in-situ concrete at the end of slabs 5 and 6.* 



*Fig. 30. Eastern end beam. Cracks in cast in-situ concrete at the end of slabs 7–9.* 



*Fig. 31. Eastern end beam. Cracks in cast in-situ concrete at the end of slabs 7–8.* 



*Fig. 32. Eastern end beam. Cracks in cast in-situ concrete at the end of slabs 8–9.* 



*Fig. 33. Eastern end beam. Cracks in cast in-situ concrete at the end of slabs 9–11.* 



*Fig. 34. Eastern end beam. Cracks in cast in-situ concrete at the end of slabs 10–12.* 



*Fig. 35. Eastern end beam. No crack in cast in-situ concrete at the end of slab 12.* 



*Fig. 36. Arrangements in reference test R1.* 

## VTT.CR.Delta.500.2005



*Fig. 37. Arrangements in reference test R1.* 



*Fig. 38. Failure in reference test R1.* 



*Fig. 39. Failure in reference test R1.* 



*Fig. 40. Failure in reference test R2.* 



*Fig. 41. Failure in reference test R2.*



## **APPENDIX B: DELTA BEAM**

*Fig. 1. Delta beam.*




























The shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

$$
V_{obs} = V_{g, sl} + V_{g, ic} + V_{eq} + V_p
$$

where *Vg,sl*, *Vg,jc*, *Veq* and *Vp* are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of loading equipment and actuator forces *Pai*, respectively. The components of the shear force due to the self-weight are calculated assuming that the slabs behave as simply supported beams. For  $V_{eq}$  and  $V_p$  the relation is  $V_{eq} = 0.8619 \times P_e$ and  $V_p = 0.8619 \times (P_{a1} + P_{a2})/2$  at failure.  $V_{q,i c}$  is calculated from the nominal geometry of the joints and density of the concrete, other components of the shear force are calculated from measured loads and weights. The values for the components of the shear force are given in Table below.

Table. Components of shear resistance due to different loads.



The observed shear resistance  $V_{obs} = 282.4$  kN (shear force at support) is obtained for one slab unit wit width =  $1,2$  m. The shear force per unit width is 235,3 kN/m.



# **10 Measured displacements**

In the following figures,  $V_p$  stands for the shear force of one slab end due to imposed actuator loads, calculated assuming simply supported slabs.

**10.1 Deflections** 





*Fig. 32. Deflection on line I along western end beam vs. support reaction V<sub>p</sub> of one slab due to actuator loads.* 



*Fig. 33. Deflection on line II in the middle of slabs 1–4.* 



*Fig. 34. Deflection on line III close to the line load, slabs 1–4.*



*Fig. 36. Deflection on line V close to the line load, slabs 5–8.* 

*Fig. 35. Deflection on line IV along the middle beam.* 



*Fig. 37. Deflection on line VI in the middle of slabs 5–8.* 









# **APPENDIX A: PHOTOGRAPHS**



*Fig. 1. Slab installed on middle beam. Fig. 2. Middle beam.*



*Fig. 3. Reinforcement at the end of middle beam. One rebar parallel to the beam on the top of the joint is still missing.*







*Fig. 4. Reinforcement at the end of middle beam. One rebar parallel to the beam on the top of the joint is still missing.*



*Fig. 5. Loading arrangements. Fig. 6. Transducers measuring deflection and differential horizontal displacement in the middle of the test floor.*



*Fig. 7. Transducers measuring differential horizontal displacement at one end of the middle beam.*



*Fig. 8. Loading of slabs 2 and 6 with two actuators*





*Fig. 11. An overview on test arrangements. Fig. 12. Failure of slab 5.*



*Fig. 9. Loading arrangements. Fig. 10. Transducers at one end of middle beam*



A634





*Fig. 15. Cracks in Western tie beam after failure. Slabs 1–3.*



*Fig. 17. Cracks in Western tie beam after failure. Slabs 3–4.*



*Fig. 13. Failure of slab 8. Fig. 14. Soffit of slabs 5–8 after failure.*



*Fig. 16. Cracks in Western tie beam after failure. Slabs 2–4.*



*Fig. 18. Cracks in Eastern tie beam after failure. Slabs 5–7.*



*Fig. 19. Cracks in Eastern tie beam after failure. Slabs 7–8.*



*Fig. 21. Failure in slabs 5–7. Fig. 22. Failure in slabs 6–8.*





*Fig. 20. Failure in slab 5.*





*Fig. 23. Failed ends of slabs 5–8. Fig. 24. Western side of middle beam. Note the failure of the bond along the vertical interface of the cast-in-situ concrete and the precast beam as well as the perfect filling of the gap below the slab end.*

![](_page_636_Picture_1.jpeg)

*Fig. 25. Western side of middle beam. Fig. 26. Eastern side of middle beam.*

![](_page_636_Picture_3.jpeg)

*Fig. 27. Overview on arrangements in reference tests. The actuators in the rear were not used.*

![](_page_636_Picture_5.jpeg)

*Fig. 29. Reference test R1. Southern side of slab after failure.*

![](_page_636_Picture_7.jpeg)

![](_page_636_Picture_9.jpeg)

*Fig. 28. Reference test R1. Northern side of slab after failure.*

![](_page_636_Picture_11.jpeg)

*Fig. 30. Reference test R2. Northern side of slab after failure.*

![](_page_637_Picture_1.jpeg)

*Fig. 31. Reference test R2. Southern side of slab after failure.*

![](_page_638_Picture_93.jpeg)

#### VTT.CR.A-beam.320.2006

![](_page_639_Figure_1.jpeg)

![](_page_640_Picture_87.jpeg)

![](_page_641_Figure_1.jpeg)

![](_page_642_Figure_1.jpeg)

![](_page_643_Figure_1.jpeg)

![](_page_644_Figure_1.jpeg)

*Fig. 12. Overview on tie reinforcement at middle beam. d xy refers to a reinforcing bar Txy, see 2.3.* 

![](_page_644_Figure_3.jpeg)

#### VTT.CR.A-beam.320.2006

![](_page_645_Figure_1.jpeg)

![](_page_646_Figure_1.jpeg)

![](_page_647_Figure_1.jpeg)














*Fig. 30. Ratio of measured support reaction of the middle beam (R<sub>p,obs</sub>) to theoretical support reaction*  $(R_{p,th})$  *vs. actuator forces on half floor.* 

The theoretical support reaction  $R_{p,th}$  is calculated from four actuator loads assuming simply supported slabs. Thus  $R_{p,th}$  is equal to (7900–1200)/7900×4x $P_{am}$  = 0,8481×4x $P_{am}$ . where  $P_{am} = (P_{at} + P_{a2})/2$ . Before failure the assumption of simply supported slabs is accurate enough to justify the calculation of the experimental shear resistance based on it.

The shear resistance of one slab end (support reaction of slab end at failure) due to different load components is given by

$$
V_{obs} = V_{g,s} + V_{g,jc} + V_{eq} + V_p \tag{1}
$$

where  $V_{q,s}$ ,  $V_{q,i}$ ,  $V_{eq}$  and  $V_p$  are shear forces due to the self-weight of slab unit, weight of joint concrete, weight of loading equipment and actuator forces *Pai*, respectively. All components of the shear force are calculated assuming that the slabs behave as simply supported beams. For  $V_{eq}$  and  $V_p$  this means that  $V_{eq} = 0.8481 \times P_e$  and  $V_p = 0.8481 \times (P_{a1} + P_{a2})/2$ .  $V_{q,p}$  is calculated from the nominal geometry of the joints and density of the concrete, other components of the shear force are calculated from measured loads and weights. The values for the components of the shear force are given in Table 1.

*Table 1. Components of shear resistance due to different loads.* 



The observed shear resistance  $V_{obs}$  = **183,3** kN (shear force at support) is obtained for one slab unit. The shear force per unit width is  $v_{obs} = 152.8 \text{ kN/m}$ 















Fig. 37. Deflection on line VII next to the line loads, slabs 5–8.



*Fig. 39. Deflection on line IX along Eastern end beam, slabs 5–8.* 



*Fig. 38. Deflection on line VIII in the middle of slabs 5–8. Transducer 46 gave erroneous results.* 



*Fig. 40. Net deflection of midpoint of middle beam (33) and those of end beams (13, 53).*





*Fig. 44. Top fibre of floor. Average strain calculated from the differential displacements shown in Figs 41–42.*

*Fig. 45. Bottom fibre of floor. Average strain calculated from the differential displacements shown in Figs 41–42.*

The variation of the average strain with the depth is illustrated in Figs 47 and 48 at the evaluated service load ( $V_p$  = 57 kN) and failure load, respectively. The mean of the average strain both for the slabs and for the beam is shown in Figs 49 and 50 at two load levels.



*Fig. 46. Average strain of slabs 2, 3, 6 and 7 as well as that of the middle beam, all in beam's direction, at estimated service load*   $(V_p = 57$  kN).

*Fig. 47. Average strain of slabs 2, 3, 6 and 7 as well as that of the middle beam, all in beam's direction, before failure at Vp = 161 kN.*

**Depth [mm]**

Depth [mm]







# **APPENDIX A: A-BEAM**



*Fig. 1. Plan and section B-B.* 



*Fig. 2. Sections A-A and C-C and list of steel parts.*

## **APPENDIX B: PHOTOGRAPHS**





*Fig. 1. A-beam. Fig. 2. A-beam. Suspension bars temporarily stored on the top of the beam.* 



*Fig. 3. Straight tie bar and bent suspension bar in their final position.*



*Fig. 5. Hollow core slabs temporarily supported on end beam. Fig. 6. Middle beam before grouting of joints.*



*Fig. 4. Detail of the previous figure.*







*Fig. 7. End of floor before grouting. Fig. 8. Test floor before grouting. Note the wedges in the joints to facilitate the demolishing of the floor after the test. To eliminate the contact between the floor and the loading frame, the outermost webs of the slabs were made thinner at the legs of the frame.*





*Fig. 11. View on the loading arrangements. Fig. 12. Loading on outermost slabs.*



*Fig. 9. Measuring devices at the end of the middle beam. Fig. 10. Measuring devices at the end of the middle beam.*





*Fig. 13. Device for measuring strain parallel to the beams.* 





*Fig. 17. Gap between soffit of slab 1 and bottom flange of middle beam.* 



*Fig. 14. Device for measuring crack width between slab end and middle beam.* 



*Fig. 15. Arrangements at end beam. Fig. 16. A general view on test arrangements.* 



*Fig. 18. Good contact between soffit of slab 4 and bottom flange of middle beam.* 



*Fig. 19. Good contact between soffit of slab 5 and bottom flange of middle beam.* 



*Fig. 21. Service load (Pa2 = 70 kN). Cracks below soffit of slabs 2 and 3.* 



*Fig. 23. Pa2 = 155 kN. Wide cracks in slab 8. Fig. 24. Cracks in slab 1 after failure.*



*Fig. 20. Good contact between soffit of slab 8 and bottom flange of middle beam.* 



*Fig. 22. Service load (Pa2 = 70 kN). Cracks below soffit of slabs 6 and 7.*





*Fig. 25. Cracks in slab 5 after failure. Fig. 26. Cracks in slab 8 after failure.*







*Fig. 27. Cracks in slab 8 after failure. Fig. 28. Cracks in Western tie beam after failure. Slabs 1 and 2.*



*Fig. 29. Cracks in Western tie beam after failure. Slabs 2 and 3.*



*Fig. 30. Cracks in Western tie beam after failure. Slabs 3 and 4. The red colour and letter A refer to an initial crack.*



*Fig. 31. Cracks in Eastern tie beam after failure. Slabs 5 and 6. The red colour and letter A refer to an initial crack.* 



*Fig. 33. Cracks in Eastern tie beam after failure. Slabs 6, 7 and 8. The red colour and letter A refer to an initial crack.* 



*Fig. 35. Cracks in slab 4 after failure. The red colour and letter A refer to an initial crack. Fig. 36. Cracks in slab 8 after failure.*



*Fig. 32. Cracks in eastern tie beam after failure. Slabs 5, 6 and 7. The red colour and letter A refer to an initial crack.* 



*Fig. 34. Cracks in Eastern tie beam after failure. Slabs 7 and 8. The red colour and letter A refer to an initial crack.*





*Fig. 37. Cracks in slab 1 after failure. The red colour and letter A refer to an initial crack.* 



*Fig. 39. Failed ends of slabs 7 and 8. Fig. 40. Failed ends of slabs 7 and 8.* 



*Fig. 41. Longitudinal cracking along joint between slabs 6 and 7.* 



*Fig. 38. Cracks in slab 5 after failure. The red colour and letter A refer to an initial crack.* 





*Fig. 42. End of slab 8 after removal of the top flange.*



*Fig. 43. A-beam after failure. The reinforcing bars have been cut after the test. Note the cement paste which has partly filled the gap between the soffit of slab 1 and the ledge of the beam.* 





*Fig. 47. Reference test R1. Southern side of slab after failure.*



*Fig. 44. A-beam after failure. Note the cement paste which has partly filled the gap between the soffit of slab 1 and the ledge of the beam.* 



*Fig. 45. Arrangements in reference tests. Fig. 46. Reference test R1. Northern side of slab after failure.*



*Fig. 48. Reference test R2. Northern side of slab after failure.*



*Fig. 49. Reference test R2. Southern side of slab after failure.* 

Arrangements and results of 20 full-scale load tests on floors, each made of eight to twelve prestressed hollow core slabs and three beams, are presented. The tests have been carried out by VTT Technical Research Centre of Finland and Tampere University of Technology.

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